

$$D = \{ \forall x \in \mathbb{R} \}$$

$$D:]-\infty; +\infty[$$

$$y = x^3 - x^2 - x + 1$$

$$y = x^2(x-1) - 1(x-1)$$

$$y = (x^2 - 1)(x - 1)$$

$$x = \pm 1$$

$$x = 1$$

	-1	1
$x^2 - 1$	+	-
$x - 1$	-	+
y	-	+

INT ASSE $y \begin{cases} x=0 \\ y=1 \end{cases} (0; 1)$

$$y' = 3x^2 - 2x - 1$$

$$\Delta = 4 + 12 = 16$$

$$x_{1,2} = \frac{2 \pm 4}{6} < \frac{1}{3}$$

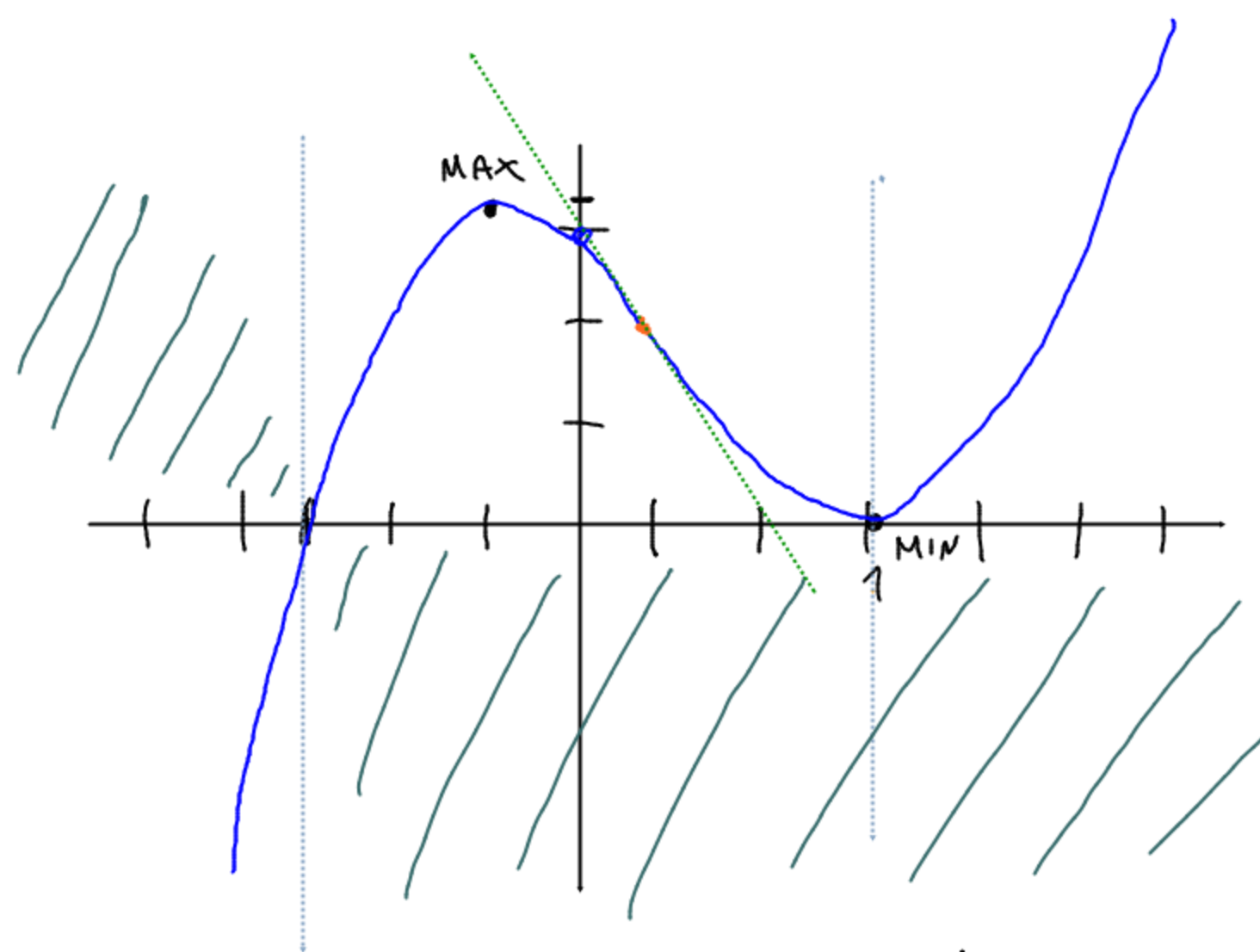
	$-\frac{1}{3}$	1
$3x^2 - 2x - 1$	+	-
y'	↗	↘
	MAX	MIN

$$y_{MAX} = f\left(-\frac{1}{3}\right) =$$

$$= \left(-\frac{1}{3}\right)^3 - \left(-\frac{1}{3}\right)^2 - \left(-\frac{1}{3}\right) + 1 = -\frac{1}{27} - \frac{1}{9} + \frac{1}{3} + 1 =$$

$$= \frac{-1 - 3 + 9 + 27}{27} = \frac{32}{27} \quad \left(-\frac{1}{3}; \frac{32}{27}\right)_{MAX}$$

$$y_{MIN} = f(1) = 1 - 1 - 1 + 1 = 0 \quad (1; 0)_{MIN}$$



$$y'' = 6x - 2$$

	$\frac{1}{3}$
$6x - 2$	-
y''	n/U

$$F\left(\frac{1}{3}\right) = \left(\frac{1}{3}\right)^3 - \left(\frac{1}{3}\right)^2 - \frac{1}{3} + 1 =$$

$$\frac{1}{27} - \frac{1}{9} - \frac{1}{3} + 1 = \frac{1 - 3 - 9 + 27}{27} = \frac{16}{27}$$

$$F\left(\frac{1}{3}; \frac{16}{27}\right)$$

TROVO L'EQ. DELLA RETTA
TANGENTE NEL FLESSO,
SI CHIAMA TANGENTE
INFLESSIONALE

$$F'\left(\frac{1}{3}\right) = 3\left(\frac{1}{3}\right)^2 - 2\left(\frac{1}{3}\right) - 1 =$$

$$\frac{3}{9} - \frac{2}{3} - 1 = \frac{3 - 6 - 9}{9} = -\frac{12}{9} = -\frac{4}{3}$$

$$y = -\frac{4}{3}x + Q$$

$$\frac{16}{27} = -\frac{4}{3}\left(\frac{1}{3}\right) + Q \Rightarrow \frac{16}{27} = -\frac{4}{9} + Q$$

$$Q = \frac{16}{27} + \frac{4}{9} = \frac{16 + 12}{27} = \frac{28}{27}$$

$$y = -\frac{4}{3}x + \frac{28}{27}$$